

A Prediction of Waste Mobiles using Holt Trends Exponential Model

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Abstract —The use of cell phones (smart phones) is quickly increasing at a great rate and correspondingly the e-waste produce from mobile is due to their short life spans. One of the factors for shorter life spans of mobile is the rapidly changing technology. In competitive mobile phone market, manufacturers are forced to add new features periodically making relatively newer phone obsolete. To support new features new hardware like sensors are added to the mobile increasing their complexity. This rapid change in mobile technology brings environmental issues since users scrap their mobile phone in a short span of time. This paper predicts the number of e-waste generated through scrapped mobile by 2024 using time series model.

Keywords-mobile scrap/trash; time series model; predict

I. INTRODUCTION

Time series analysis is generally used for a group of observations derived by calculating at regular intervals in a time span. It depicts the historical report which changes over a time. This paper suggests Holt's Trend Exponential Smoothing model for e-waste prediction due to scrapped mobile phone. Time series model have the smoothing boundary which are level and trend that are not saved by each other significance. It is known to be suitable for a series when seasonality is not therein data set and it consist of a linear trend

II. DATA COLLECTION

IDC publishes data every after three month cell phones sales data and the salesperson in India. This data / (report) was used as a secondary data / (report) source for the cell phones sales data in India. Source [IDC]

Table 1: Data of mobile sales (in millions)

Quarterly data in millions				
Year	Q1	Q2	Q3	Q4
2010	25.53	38.63	40.08	45.76
2011	62.4	42.8	44.92	29.88
2012	48.8	51.24	42.82	57.14
2013	60.73	62	60.44	61.83
2014	60.05	63.21	72.5	74.24
2015	60.05	63.21	72.5	74.24
2016	52.8	61.2	72.3	58.7
2017	62.22	62	80	56
2018	54.3	74.2	82.2	68.5
2019	64.4	69.3	85	67
2020	55.3	28.2	80	43.9
2021	38			

The research shows that 32.92 % mobiles are refurbished, 29.59 % are recycled and 37.48% are scrapped. [2] After applying 37.48% scrapped percentage on the above data, the scrapped mobiles mobile data was calculated. This is input data for Holt trend Time series model.

Table 2 : Data of Scrapped mobiles(in millions)

	Qtr1	Qtr2	Qtr3	Qtr4
2010	10.30700	10.30700	10.30700	10.30700
2011	15.57406	15.57406	17.30798	17.30798
2012	15.26643	20.17631	20.04769	23.79289
2013	29.98722	23.87406	26.70781	19.05836
2014	27.08245	25.47877	24.96448	29.80368
2015	30.97991	33.04897	32.85150	34.05361
2016	33.32145	34.90155	38.14242	39.31474
2017	35.06323	36.63352	38.71581	39.88491
2018	32.53469	36.06787	37.80846	33.87430
2019	35.76660	34.38902	41.75836	32.30967
2020	34.09849	38.44650	42.03378	38.33039
2021	37.97464			

III FRAMEWORK AND ITS VERI FICA TION

Linear trend model is been described by a time series getting high or low at a fixed range

$$y_t = \beta_0 + \beta_1 t + \varepsilon_t$$

Holt's trend exponential smoothing model can be used for time series survey when there is the change in boundary value of β_0 and β_1 over a time

Note; Regression is been used when there is no change in the boundary value of β_0 or β_1 over a time T :

$\beta_0 + \beta_1 T$ is known as the level at a time

β_1 is known as the growth rate

IV Holt's Trend Exponential Smoothing model

Exponential smoothing model is used when the time series shows no trend. Holts model makes it possible to apply exponential smoothing to the time series data with trend.

The forecast equation is given by,

$$\hat{y}_{T+h|T} = l_T + hb_T$$

Where

l_T is the level & b_T is the trend estimate.

Level estimate

$$\ell_T = \alpha y_T + (1 - \alpha)(\ell_{T-1} + b_{T-1})$$

Trend estimate

$$b_T = \gamma(\ell_T - \ell_{T-1}) + (1 - \gamma)b_{T-1}$$

$\alpha = 0 \leq \alpha \leq 1$ [Denoted as constant for level]

$\gamma = 0 \leq \gamma \leq 1$ [Denoted as constant for trend]

Steps for the above method are as follow

Step 1: By connecting a least square trend lines to half of the past report obtain the estimates value of ℓ_0 and b_0

Step 2: Calculate the value of y_1 from time 0.

Step 3: Change the value of ℓ_T and b_T by using some pre-establish values of constant.

Step 4: Search the ideal integration for α & γ to reduce MSE / SSE

V THE PREDICTION MODEL

R code applied on the data produces the following results

Forecast method: Holt's method

Model Information:

Holt's method

Call: holt(y = AutoSales, h = 15)

Smoothing parameters:

$\alpha = 0.3397$

$\gamma = 0.0365$

Initial states:

$l = 8.4126$

$b = 1.0778$

sigma: 3.3192

AIC : 285.0853

AICc : 286.6237

BIC: 294.1186

Error measures(Training set):

ME -0.4918501

RMSE 3.168226

MAE 2.350411

MPE -2.441372

Website: <http://www.modern-journals.com/>

MAPE 9.06642

MASE 0.8177214

ACF1-0.01292697

Level estimate

$\ell T = 0.3397 yT + 0.6603 (\ell T - 1 + b T - 1)$

Trend estimate:

$bT = 0.0365 (\ell T - \ell T - 1) + 0.9635 bT - 1$

Forecasts:

Point Hi 95	Forecast	Lo 80	Hi 80	Lo 95
2021-Q2 32.42115	38.92661 45.43208	34.67292	43.18031	
2021-Q3 32.24563	39.19616 46.14670	34.65145	43.74088	
2021-Q4 32.01467	39.46571 46.91675	34.59374	44.33769	
2022-Q1 31.73164	39.73527 47.73889	34.50197	44.96856	
2022-Q2 31.39999	40.00482 48.60964	34.37842	45.63121	
2022-Q3 31.02311	40.27437 49.52563	34.22529	46.32344	
2022-Q4 30.60414	40.54392 50.48370	34.04464	47.04319	
2023-Q1 30.14594	40.81347 51.48100	33.83834	47.78859	
2023-Q2 29.65106	41.08302 52.51497	33.60806	48.55797	
2023-Q3 29.12178	41.35257 53.58336	33.35528	49.34985	
2023-Q4 28.56007	41.62212 54.68416	33.08131	50.16293	
2024-Q1 27.96770	41.89167 55.81563	32.78728	50.99606	
2024-Q2 27.34621	42.16122 56.97623	32.47421	51.84823	
2024-Q3 26.69695	42.43077 58.16459	32.14298	52.71856	
2024-Q4 26.02114	42.70032 59.37950	31.79439	53.60625	

Table 3 : Forecast of Scrapped mobiles(in millions)

The above table displays the forecast values upto 4th quarter of 2024. It also shows high and low values with 80% and 95% confidence levels.

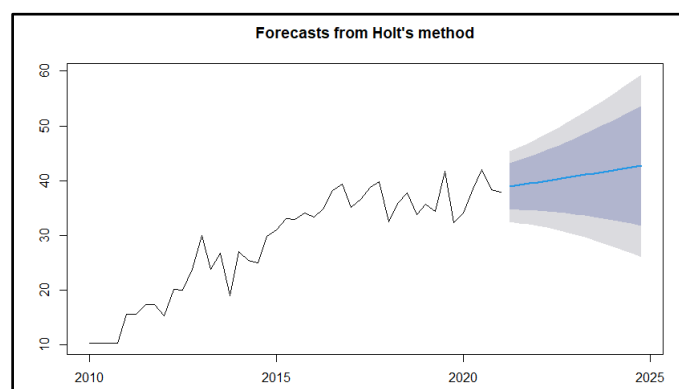


Figure 1: forecast from Holts method

In this figure we can visualize the trend of the current data and the forecast. The forecast shows upward trend.

Let us understand the forecast model with the help of various error measures.
 Analysis of the error measures:

RMSE (Root Mean Square Error): RMSE defines the difference between model-predicted level and the dependent series.

RMSE value (variation) in this case is 3.168226 which is relatively low.

MAPE (Mean Absolute Percentage Error): MAPE used to determine how much a series differs from its predicted series. MAPE value (variation) in this case is 9.06642.

MAE (Mean absolute error): MAE used to calculate how much a series differs from its model-predicted level.

Mean absolute error is reported in the original series units.

MAE value (variation) in this case is 2.350411.

ACF1 Autocorrelation of errors at lag 1.

It is a measure of how much the current value is influenced by the previous values in a time series. The correlation between a point and the next point is -0.01292697. Which is almost no correlation.

Test for model validity : Ljung-Box test

The Ljung Box test is a way to test for the serial autocorrelation, up to a specified lag k .

The test determines whether or not errors are Independent and Identically Distributed. It checks whether or not the autocorrelations for the errors or residuals are non zero. It is a test of lack of fit: if the autocorrelations of the residuals are very small, then the model doesn't show 'significant lack of fit'.

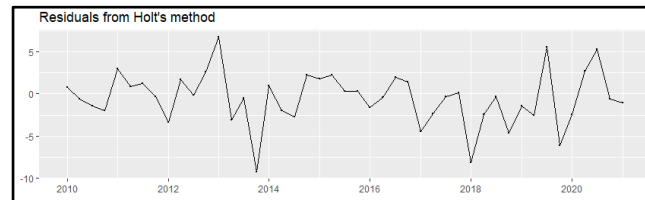


Figure 2: Residuals from Holts method

The Hypothesis of the Box Ljung Test is as follows,

H_0 , is that our model *does not* show lack of fit.

H_a , is just that the model *does* show a lack of fit.

Also based on p value,

If **p-value** < 0.05: You can reject the null hypothesis assuming a 5% chance of making a mistake.

If **p-value** > 0.05: You don't have enough statistical evidence to reject the null hypothesis.

Test performed on the forecast yields the following:

Residuals from Holt's method

$Q^* = 8.5732$,

df = 5,

p-value = 0.1273

Model df: 4. Total lags used: 9

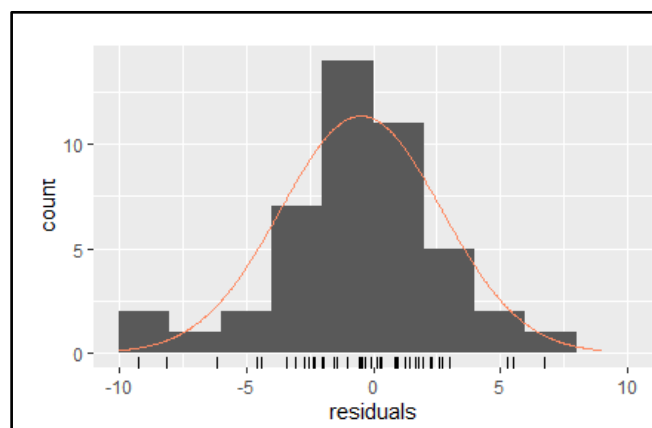


Figure 3: histogram

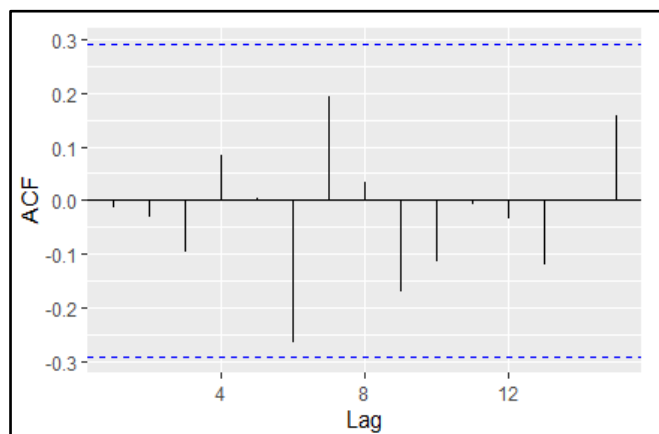


Figure 4: First order autocorrelation

p-value = 0.1273 thus,
since **p-value** > 0.05:

We don't have enough statistical evidence to reject the null hypothesis.

Thus we accept the null hypothesis.

Thus the forecasted model does not show lack of fit.

VI CONCLUSION

Applying Holt's trend time series to forecast the expected scrap for the future years was performed. The model was validated and shows a good fit as per As per Box Ljung Test. the graph in figure 1 shows that there is upward trend in time series, In the above data set, 42.7 million e-waste is forecasted value of scrap for the fourth quarter of year 2024 with maximum value of 59.37 million and minimum value of 26.02 million. with this forecast it becomes possible to take proper steps to handle the scrap generated.

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